



HEAF Modeling with Sierra

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Sierra Plasma Arc Modeling



The conduction of current through the gas (arc) is the source of gas heating, melting and vaporization of metal, and radiation.

The NIST simulation software Fire Dynamics Simulator (FDS) has expertise in gas heating and transport mechanisms but does not have a capability for accurate modeling of the arc physics.

Sandia National Laboratories (SNL) has extensive capability and expertise in simulating arc physics. Scales for arc physics are micron (and smaller) and require accurate modeling of charged particle transport to capture localized heating effects.

The current approach is to use a Sierra model for the arc and local gas transport, then transfer results to FDS for the full domain transport problem.



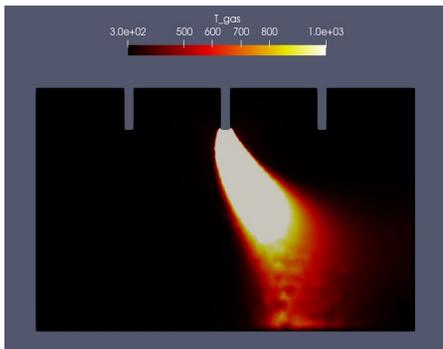
Arc domain

(walls removed for viewing cabinet internals)

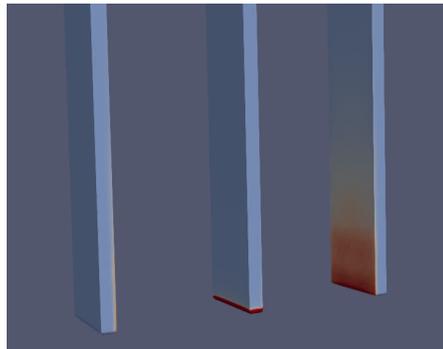
HEAF – a Complex Multi-scale Coupled Physics Problem



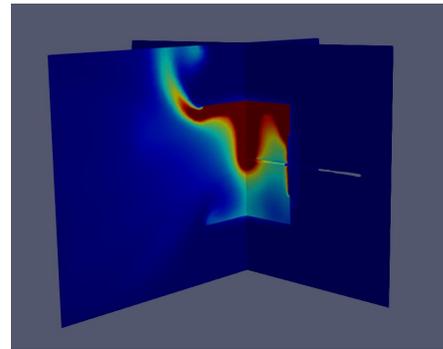
Arc Physics
(μm scale)



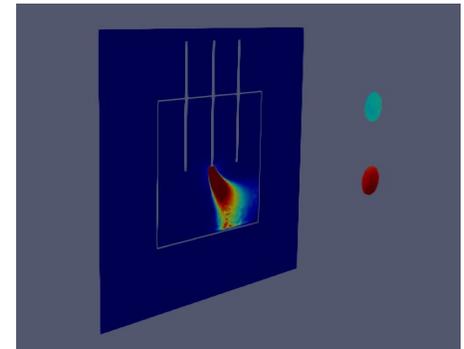
Electrode Melting/Vaporization
(mm scale)



Gas Heating
(cm-to-m scale)



Radiation
(m scale)



Feedback from different phenomena lead to a coupled physics problem

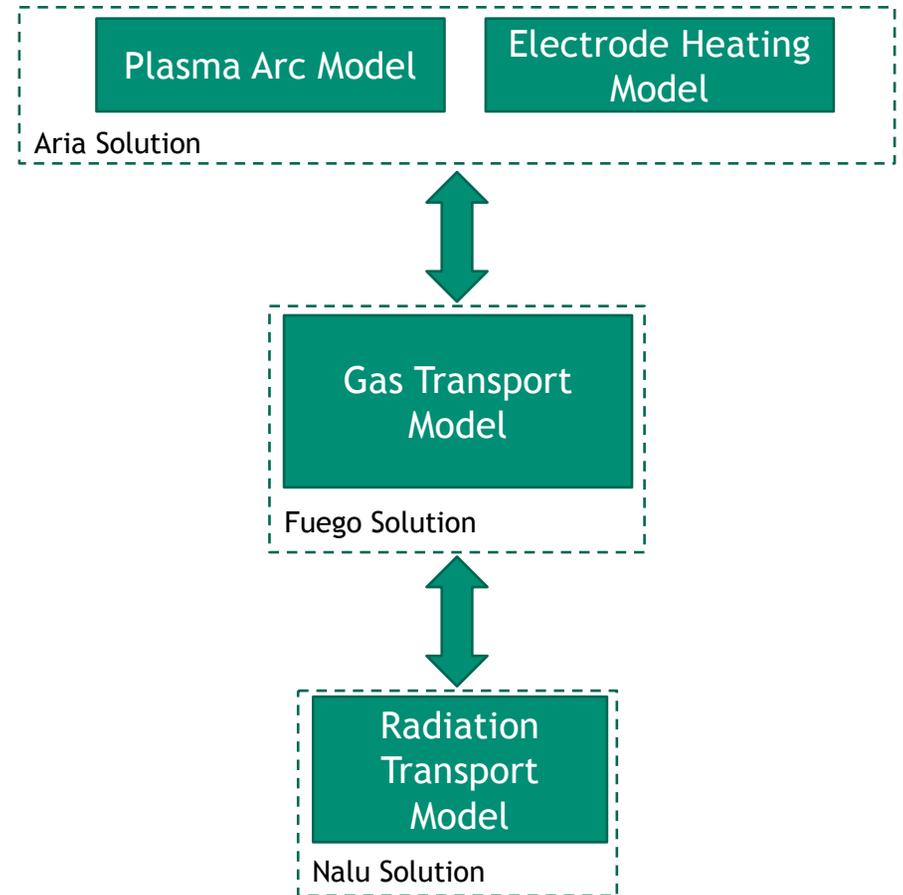
Arc Model Overview



The Sierra model couples together hydrodynamics (Fuego), plasma physics (Aria), and radiation transport (Nalu).

It is possible to investigate differences in electrode materials, gas composition, gas optical thickness, and other parameters, depending on resource allocation.

The model currently assumes a DC plasma discharge (providing time-averaged heating rates).





Fully-coupled Model Equations

Gas dynamics

$$\frac{\partial \rho}{\partial t} + \rho \nabla \cdot \mathbf{v} + \mathbf{v} \cdot \nabla \rho = q_m \quad \text{(continuity)}$$

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho \mathbf{v} \nabla \cdot \mathbf{v} - \mathbf{g} - \nabla \mathbf{T} = 0 \quad \text{(momentum)}$$

$$\frac{\partial(\rho C_p T)}{\partial t} + \rho C_p \mathbf{v} \cdot \nabla T = -\nabla \cdot \mathbf{q} + H_v \quad \text{(energy)}$$

1-term turbulence model equation
Species transport (Al/Cu)

Plasma arc (drift-diffusion approximation)

$$\frac{\partial n_x}{\partial t} + \nabla \cdot \Gamma_x = S_e \quad \text{(charged species continuity)}$$

$$\Gamma_x = \pm \mu_x n_x \mathbf{E} - \nabla(n_x D_x) \quad \text{(flux term)}$$

$$\nabla^2 \varphi = \frac{-e(n_e - n_i)}{\epsilon_0} \quad \mathbf{E} = -\nabla \varphi \quad \text{(electrostatic voltage and electric field)}$$

$$H_v = \mathbf{J} \cdot \mathbf{E} \quad \mathbf{J} = \sigma \mathbf{E} \quad \sigma = n_e \mu_e e$$

(Heating/Coupling between equations)



Radiation transport

$$s_i \frac{\partial}{\partial x_i} I(s) + \mu_a I(s) = \frac{\mu_a \sigma T^4}{\pi} \quad \text{(transport)}$$

$$I(s) = \frac{1}{\pi} [\tau \sigma T_\infty^4 + \epsilon \sigma T_w^4 + (1 - \epsilon - \tau) q_j^{r,inc} n_j] \quad \text{(boundaries)}$$

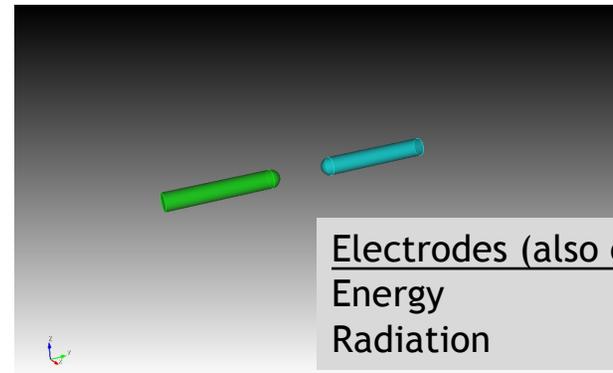
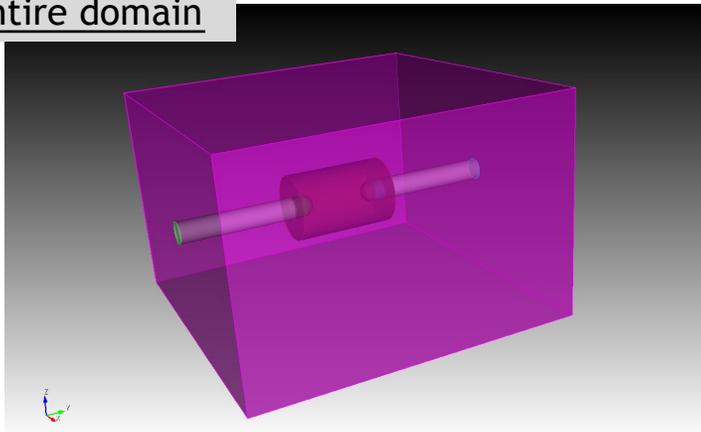
$$\frac{\partial q_i^r}{\partial x_i} = \mu_a [4\sigma T^4 - G] \quad \text{(energy source)}$$

When solving the current density self-consistently, we employ mean energy = 3/2kT for Bolsig+ to compute f(mean energy) transport quantities.

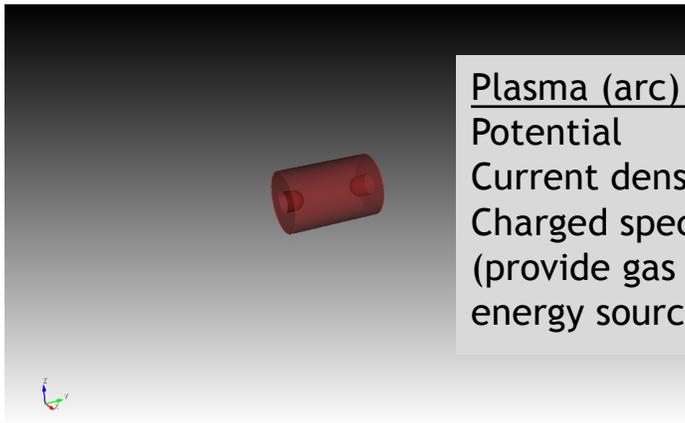
Example Coupled Problem



Entire domain

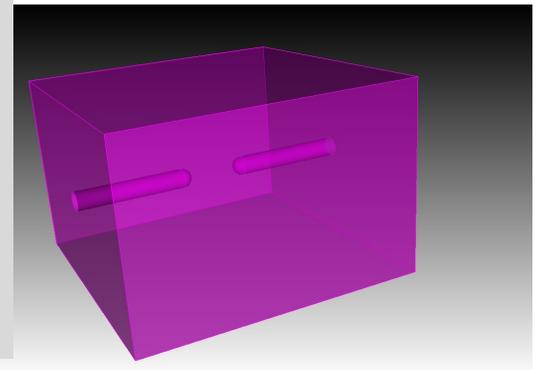


Electrodes (also calorimeters)
Energy
Radiation

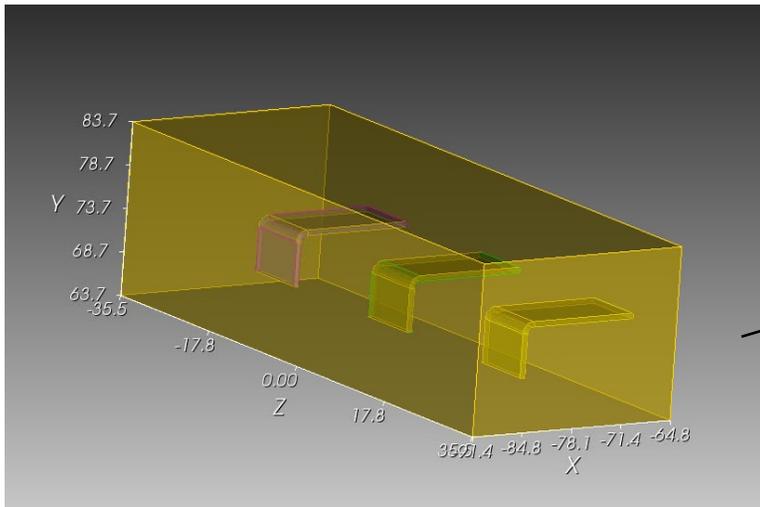


Plasma (arc) region
Potential
Current density
Charged species
(provide gas region
energy source term)

Gas region
Mass
Momentum
Turbulent kinetic energy
Energy
Radiation (Nalu)
(provide plasma region
temperature)

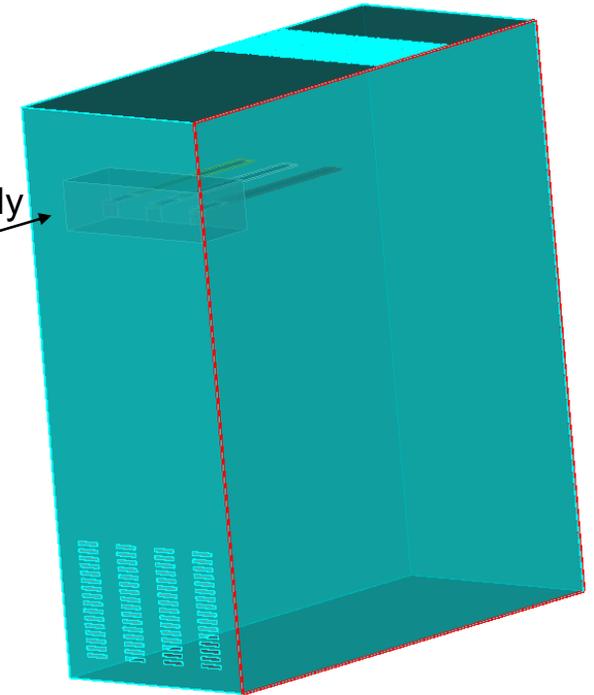


Medium Voltage Switchgear Simulations – 2018 KEMA Test



No metal or combustion reaction included

Focus on plasma region only



Nominal parameters:

- 6900 V L-L system voltage
- 25.76 kA
- 246 V L-N arc voltage
- 2 s duration

Model setup:

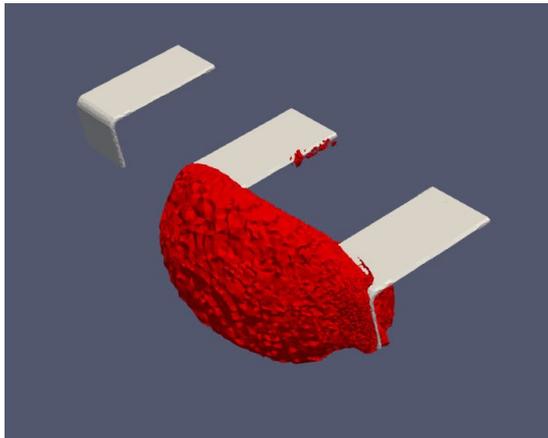
- Injection of 25.76 kA (electron current) from middle electrode to right electrode.
- Middle and left electrode fixed at -246 V.
- Other electrode and surfaces at ground.

Localized Heating

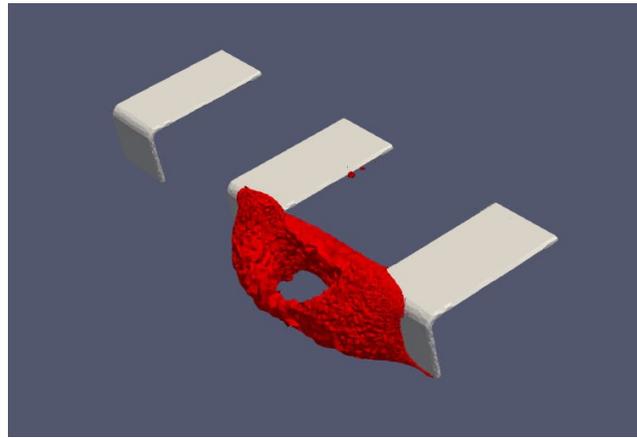


Locations of gas heating due to arc (plasma) formation.

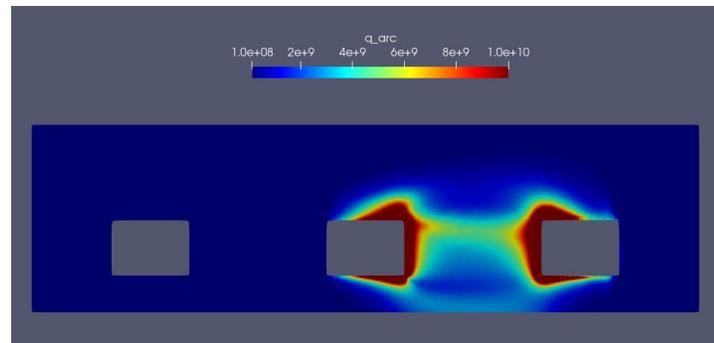
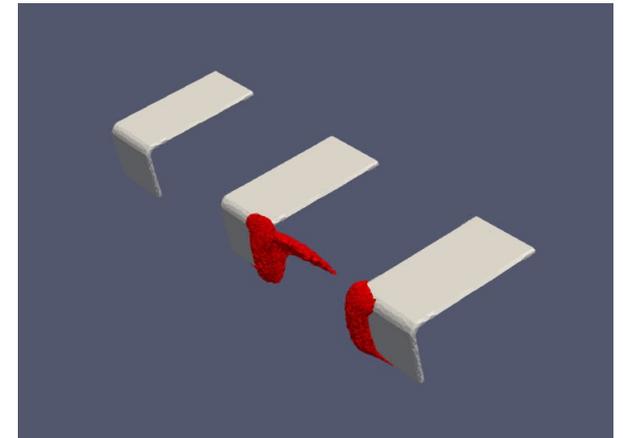
90% total



50% total

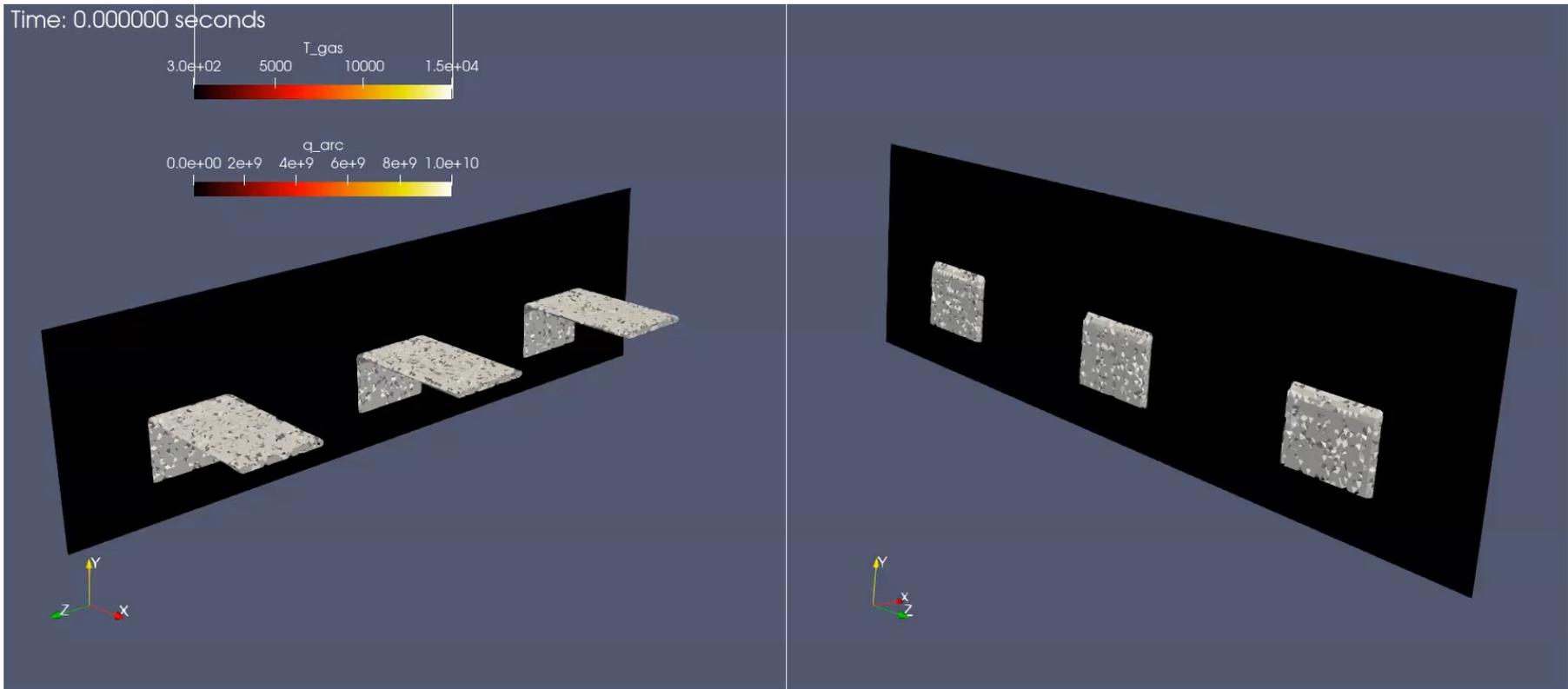


10% total



NRC 2018 KEMA Test

Evolution of gas temperature and heating source



NRC 2018 KEMA Test

“Current” Activity

Complete Al Oxidation Reaction

- $\text{Al} + \text{O}_2 \rightarrow \text{AlO} + \text{O}$

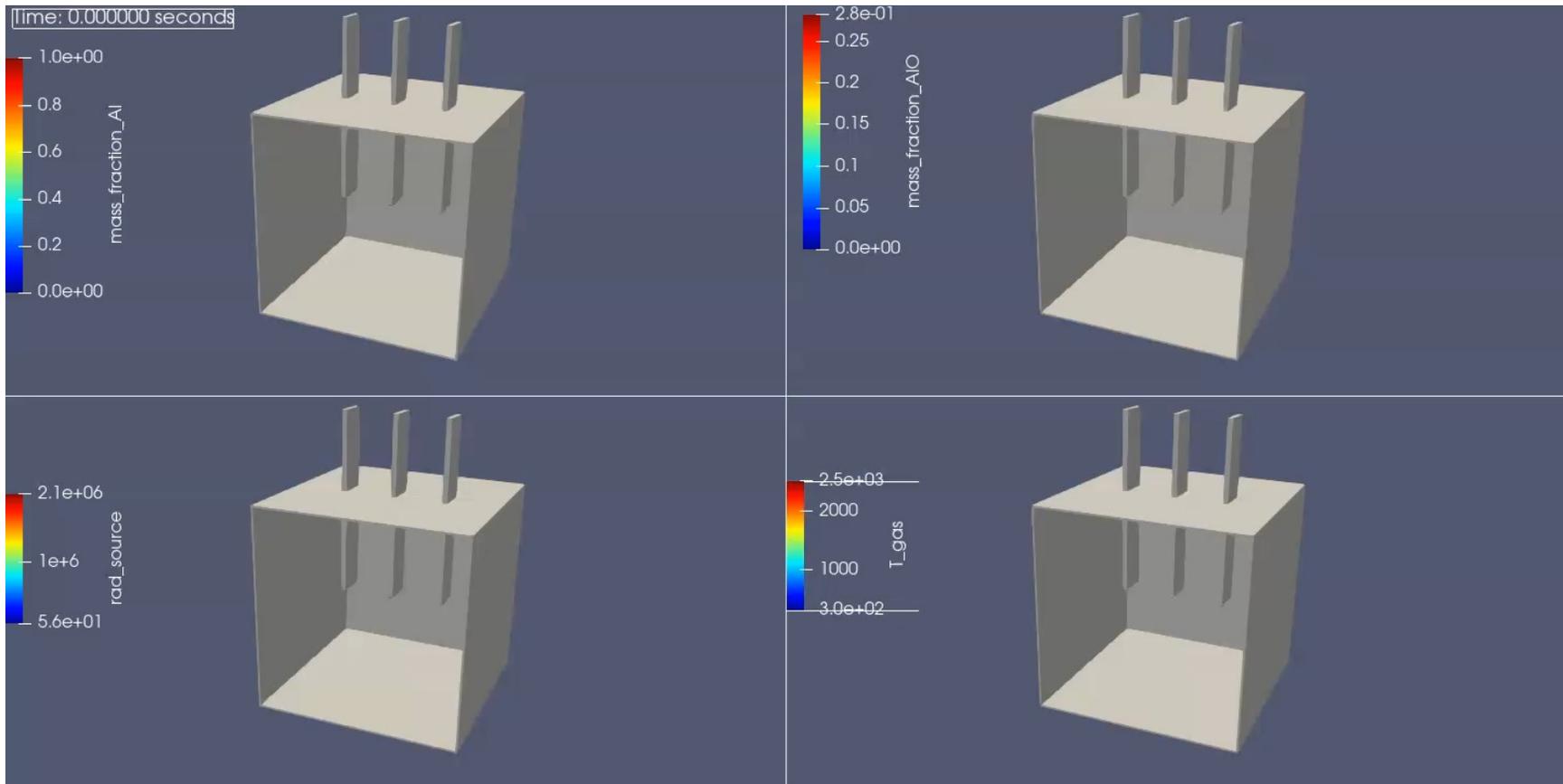
Continue definition of hand-off parameters for plasma arc source term to FDS model

- Power
- Radiation fraction
- Compare temperatures between FDS and Sierra

Develop other geometries and operating conditions for ZOI calculations



AIO Reaction Included



AIO Reaction Included

